A. S. Kechris: Global Aspects of Ergodic Group Actions; Corrections and Updates (January 16, 2018)

Page x, line 3: Replace "the equivalence" by "an ergodic equivalence".

Page 8, last 7 lines of the proof of 2.5: Replace ξ_i by η_i .

Page 12, line 3-: Add "." at the end.

Page 19, Theorem 3.13: This was originally proved in H.A. Dye, On groups of measure preserving transformations, I, Amer. J. Math., 81(1) (1959), 119–159.

Page 20, Theorem 4.1: This was originally proved in H.A. Dye, On groups of measure preserving transformations, II, *Amer. J. Math.*, **85(4)** (1963), 551–576.

Page 22, line 20-: François Le Maître pointed out that in [BG1] the authors prove this result for the class of measure-class preserving equivalence relations but the older result for the case of measure preserving equivalence relations is due to H.A. Dye, On groups of measure preserving transformations, II, Amer. J. Math., 85 (1963), 551–576, Proposition 5.1.

Page 26: An update concerning the results in the paragraph following 4.12: Matui has shown that for ergodic hyperfinite E, t([E]) = 2, and $t([E_n]) \le 2(n+1)$. Independently Marks also proved that t([E]) = 2 and moreover showed that $t([E_n]) \le 2n$ and if E_n is induced by a free modular action of F_n , then $t([E_n]) = n + 1$.

Finally Le Maître proved that for every ergodic measure preserving E one has the formula $t([E]) = \lfloor C_{\mu}(E) \rfloor + 1$, where $\lfloor C_{\mu}(E) \rfloor$ is the integer part of the cost of E, and therefore $t([E_n]) = n + 1$. He also obtained a related formula when E is aperiodic but not necessarily ergodic.

Page 30, line 1-: After "3.14" add "and 2.6".

Page 67, line 18: Delete "ergodic".

Page 71, 10.9: Add in the statement of the theorem that Γ is an infinite countable group.

Page 71, line 4: Before "Let" add "By 10.8, we can assume that a is free".

Page 71, line 11: Replace "The extreme ... Krein-Milman" by "Using the ergodic decomposition of a and the fact that a is free, we see that".

Page 71, line 13: After "ergodic," add "and non-atomic,".

Page 73, line 7-: Replace "iff" by " \Longrightarrow ".

Page 73, line 1-: Replace " $\Gamma \leq Z(\Delta)$ " by " $\Gamma \leq C_{\Delta}(T)$ = the centralizer of T in Δ ".

Page 75, Remark: Robin Tucker-Drob answered the question at the end of this remark by showing that $C^*(\Gamma) = C^{**}(\Gamma)$ for all infinite groups Γ . The proof is as follows:

It is enough to show that if Γ has property (T), then $C(\Gamma) = C^*(\Gamma) = C^{**}(\Gamma)$. Indeed, suppose that Γ has property (T). Then Γ is finitely generated (see [BdlHV, 1.3.1]), so by Corollary 10.14 we have $C(\Gamma) = C^*(\Gamma)$. It remains to show that $C(\Gamma) = C^{**}(\Gamma)$. By Theorem 13.1 the set A, consisting of all actions $a \in \operatorname{FRERG}(\Gamma, X, \mu)$ with weakly dense conjugacy class in $\operatorname{FRERG}(\Gamma, X, \mu)$, is dense G_{δ} in $(\operatorname{FRERG}(\Gamma, X, \mu), w)$. Fix $a \in A$. Let $b \in \operatorname{FR}(\Gamma, X, \mu)$ and let $\mu = \int_{Z} \mu_{z} d\eta(z)$ be the ergodic decomposition of b, so η -almost every measure μ_{z} is b-invariant and ergodic. Let b_{z} denote the action of Γ on (X, μ_{z}) , so that b_{z} is almost surely ergodic. Since b is free, η -almost every b_{z} is free. Hence, for η -almost every $z \in Z$ we have $b_{z} \prec a$. This implies $b \prec i_{Z} \times a$, where i_{Z} is the identity action of Γ on (Z, η) . Since Γ is finitely generated Corollary 10.14 gives $C(i_{Z} \times a) \leq C(b)$; since $C(i_{Z} \times a) = C(a)$, we have have $C(a) \leq C(b)$. As $b \in \operatorname{FR}(\Gamma, X, \mu)$ was arbitrary, this shows that $C(a) = C(\Gamma)$. Since $a \in A$ was arbitrary and $a \in A$ is dense $a \in A$ in $a \in A$ i

Page 79, lines 4-5: R. Tucker-Drob, Shift-minimal groups, fixed price 1, and the unique trace property, arXiv: 1211.6395v3, Corollary 6.22, shows that for infinite Γ and $a \prec b$, a free:

$$C(b) < \infty \implies C(b) \le C(a),$$

$$E_b$$
 treeable $\implies C(b) \leq C(a)$.

Page 87, line 18: Add ")" at the end of the formula.

Page 90, 12.11: Replace [HJ4] by [HJ5].

Page 90, Proof of 13.1: Here view (by picking representatives) the a_n , a as Borel actions and not equivalence classes of Borel actions up to equality a.e.

Page 91, last Remark: Add:

It is shown in D. Kerr and H. Li, *Ergodic Theory*, Springer, 2016, Theorem 4.45, using the results of D.S. Ornstein and B. Weiss, Entropy and isomorphism theorems for actions of amenable groups, *J. Analyse Math.* 48 (1987), 1–141, that if Γ is amenable, then every action in $FR(\Gamma, X, \mu)$ has dense conjugacy class in $(FR(\Gamma, X, \mu), u)$.

Page 114, line 9-: Replace "lemma" by "theorem".

Page 123, line 7-: add "sofic" before Γ .

Page 123, (IIIb) and (IVb): G. Hjorth and A. Törnquist, The conjugacy relation on unitary representations, *Math. Res. Lett.*, 19(3) (2012), 525–535, have shown that unitary equivalence for any Γ is Borel, in fact Π_3^0 .

In E. Gardella and M. Lupini, The complexity of conjugacy, orbit equivalence, and von Neumann equivalence of actions of nonamenable groups, arXiv:1708.01327v2, it is shown that isomorphism and orbit equivalence on free, ergodic (in fact even weak mixing) actions are not Borel for all non-amenable groups.

Page 131, 3 lines before (B): generically \rightarrow generally.

Page 141, line 4 of the proof of 21.4: add period.

Page 184, last lines of 30.4, 30.5: G-superrigid \rightarrow G-cocycle superrigid.

Page 185, third line of 30.6: G-superrigid \rightarrow G-cocycle superrigid.

Page 186, 10-: F_2 -superrigid $\rightarrow F_2$ -cocycle superrigid.

Page 186, 2-: G-superrigid \rightarrow G-cocycle superrigid.

Page 208, line 7 of (B): positive definite \rightarrow positive-definite.

Page 214, line 14: After "claim" add "applied to e_1, \ldots, e_p and a given open set $W' \subseteq W$ ".

Page 234: add to index i_{Γ} , 67